

Origin of the ESR spectrum in the Prussian blue analog $\text{RbMn}[\text{Fe}(\text{CN})_6] \cdot \text{H}_2\text{O}$

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We present an electron spin resonance (ESR) study at excitation frequencies of 9.4 and 222.4 GHz of powders and single crystals of a Prussian blue analog (PBA), $\text{RbMn}[\text{Fe}(\text{CN})_6] \cdot \text{H}_2\text{O}$ in which Fe and Mn undergoes a charge-transfer transition between 175 and 300 K. The ESR of PBA powders, also reported by Pregelj *et al.* [*J. Magn. Magn. Mater.* **316**, e680 (2007)], is assigned to cubic magnetic clusters of Mn^{2+} ions surrounding $\text{Fe}(\text{CN})_6$ vacancies. The clusters are well isolated from the bulk and are superparamagnetic below 50 K. In single crystals, various defects with lower symmetry are also observed. Spin-lattice relaxation broadens the bulk ESR beyond observability. This strong spin relaxation is unexpected above the charge-transfer transition and is attributed to a mixing of the Mn^{3+} - Fe^{2+} state into the prevalent Mn^{2+} - Fe^{3+} state.

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I. INTRODUCTION

The interest in the extensively studied Prussian blue analogs (PBAs), $A(\text{I})M(\text{II})[N(\text{III})(\text{CN})_6]$, where $A = (\text{Na}, \text{K}, \text{Rb}, \text{Cs})$; $M = (\text{Mn}, \text{Co}, \text{Cr})$; $N = (\text{Fe}, \text{Cr})$, lies in a charge-transfer transition between high-temperature (HT) and low-temperature (LT) phases.^{2,4,5} Besides a temperature change, the transition can be triggered by illumination with visible light⁶⁻⁸ or x rays⁹ and also by application of pressure.⁷ The materials have potential technological applications such as magneto-optic devices based on photoinduced magnetism.

In the compound studied in this paper, $\text{RbMn}[\text{Fe}(\text{CN})_6] \cdot \text{H}_2\text{O}$, the HT phase is cubic ($F\bar{4}3m$; $Z = 4$) with Mn^{2+} and Fe^{3+} ions in $S = 5/2$ and $S = 1/2$ spin states respectively. The LT Mn^{3+} ($S = 2$), Fe^{2+} ($S = 0$) phase has a tetragonal symmetry ($I\bar{4}m2$; $Z = 2$). The charge-transfer transformation is driven by a Jahn-Teller distortion of Mn^{3+} ions.² The transition has a broad thermal hysteresis with the LT \rightarrow HT transition at approximately 300 K and the HT \rightarrow LT transition at about 175 K.¹ In the LT phase, below $T_F = 11$ K the $S = 2$ spins of the Mn^{3+} ions order ferromagnetically.^{10,11}

In the present detailed study of single crystals and powder PBA samples, we discuss the origin of electron spin resonance (ESR) active defects and set a lower limit for the unusually fast spin relaxation rate in the bulk. The experimental findings in powders are in good agreement with the study of Pregelj *et al.*¹² We assign an isotropic ESR line to a cubic cluster (denoted hereafter “C-cluster”) of Mn^{2+} ions surrounding the structural defect shown in Fig. 1 and described earlier by Vertelman *et al.*¹ The C-clusters are remarkably well isolated from the bulk and are only little affected by the HT-LT charge-transfer transition. At low temperatures, C-clusters remain superparamagnetic even below the ferromagnetic Curie temperature of the bulk, at $T_F = 11$ K. In

single crystals, defects with lower symmetry are also observed. We find no ESR of the bulk in spite of an intensive search; spin-relaxation broadening of the line is more than 1 T. The lack of a bulk ESR in the high-temperature phase is surprising as the $S = 5/2$ spin Mn^{2+} and the $S = 1/2$ Fe^{3+} ions are usually easily observed. We argue that an admixture of the Mn^{3+} - Fe^{2+} state into the Mn^{2+} - Fe^{3+} state is the reason for the fast spin relaxation in the HT phase.

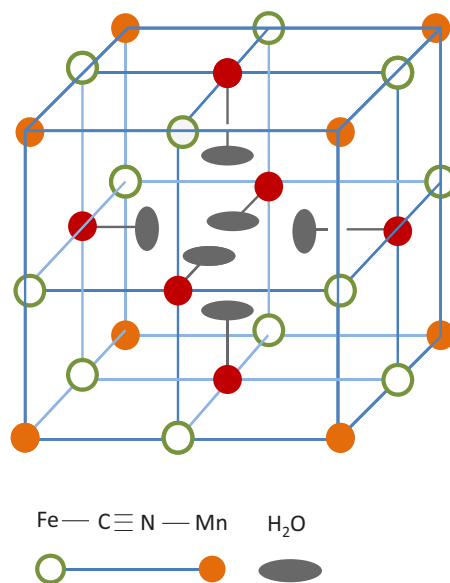


FIG. 1. (Color online) Structure of a cubic Mn^{2+} cluster in $\text{RbMn}[\text{Fe}(\text{CN})_6] \cdot \text{H}_2\text{O}$ surrounding an $\text{Fe}(\text{CN})_6$ vacancy. Rb^+ ions and noncoordinated lattice water molecules are omitted for clarity (Ref. 13). The six Mn^{2+} ions of the cluster (darker) have five Fe first neighbors unlike the Mn ions of the bulk (lighter) that have six Fe first neighbors.

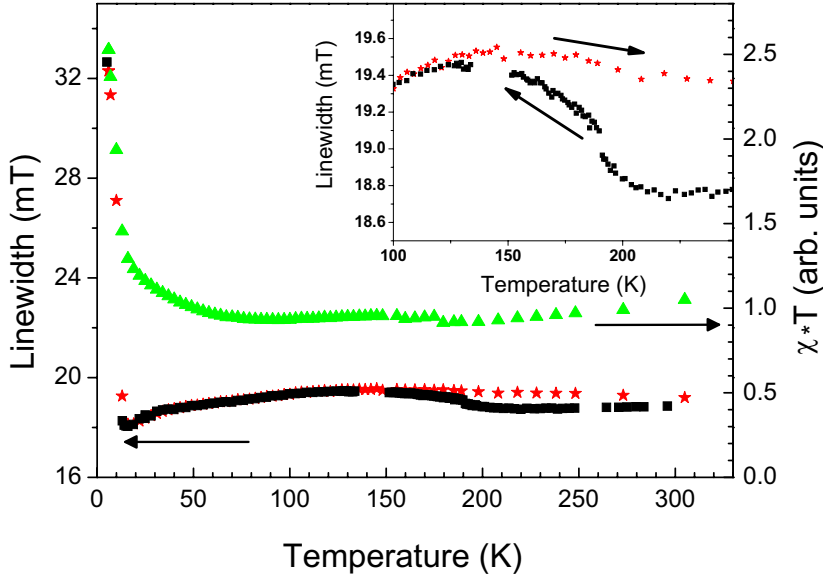


FIG. 2. (Color online) 9.4 GHz ESR linewidth (stars: heating, cubes: cooling) and ESR susceptibility times temperature (triangles) of PBA powder sample as a function of temperature. Inset: hysteresis of the linewidth at the HT→LT transition.

II. EXPERIMENTAL RESULTS

The $\text{RbMn}[\text{Fe}(\text{CN})_6] \cdot \text{H}_2\text{O}$ single crystals are from the same batch as in Ref. 1; details of the synthesis and characterization are given in the Appendix. Measurements at 222.4 GHz were performed by a home-built ESR spectrometer while at 9.4 GHz we used a Bruker ELEXSYS E500 spectrometer. The sample was annealed at 320 K before thermal cycling experiments to ensure that it was fully in the high-spin state. In this section, we first present the experimental results on ESR-active defect sites in powder samples, we continue with the findings in single crystals, finally we give a lower limit to the ESR linewidth of the bulk.

A. ESR in powder samples

In powdered samples, a single strong ESR line is observed at both 9.4 and 222.4 GHz and at all temperatures between 4 and 320 K.

The intensity of the ESR line, which is proportional to the spin susceptibility of the ESR-active species, was measured at ambient temperature in a powder sample at 9.4 GHz using $\text{CuSO}_4 \cdot 5\text{H}_2\text{O}$ reference. The ESR intensity of the powder sample corresponds to a concentration of about 2.5% of Mn^{2+} ions; a similar concentration was reported in Ref. 12. This is much less than expected for a resonance arising from one $S=5/2$ Mn^{2+} paramagnetic ion per formula unit. A line with so small intensity cannot arise from the ESR of the bulk, only from defect sites.

The defects with isotropic ESR were observed in powders at both frequencies and all temperatures. At room temperature, the linewidth of the defects, ΔH , in the powder is almost independent of the Larmor frequency, ν_L . On the other hand, the g -factor of the powder has a curious frequency dependence, it varies from $g=2.022$ at $\nu_L=9.4$ GHz to 2.0006 at 222.4 GHz. The HT-LT transition affects only weakly the ESR signal of the defect sites. The line is slightly narrower in the HT phase than in the LT phase, and there is a small hysteresis in the linewidth between 175 and 300 K (Fig. 2 inset). Within experimental accuracy, the ESR inten-

sity follows a Curie law (Fig. 2) between 50 and 300 K, it is not affected by the HT-LT transition. On the other hand, the spin crossover is clear in static magnetization measurements of similar powders. We conclude that there is no spin crossover in the magnetic ions of the ESR-active defect sites.

The defect is not a single isolated magnetic ion. Below 50 K, the ESR magnetic spin susceptibility increases faster than predicted by the Curie law and at 5 K, it is several times larger than expected for a constant concentration of free spins.

The 9.4 GHz ESR line slightly narrows below 50 K and then increases rapidly as the sample is cooled below the ferromagnetic ordering temperature of the bulk at 11 K (Fig. 2). At 222.4 GHz, the line starts to broaden already at 25 K, i.e., at a much higher temperature than in low magnetic field.

B. ESR in single crystals

As in powders, there is no intense resonance of the bulk in the superior sample quality single crystals. However, unlike in powders, in single crystals two types of ESR-active defects appear with isotropic and anisotropic g -factors. Three resonances were clearly resolved with different linewidths and resonance fields in the single crystal, 9.4 GHz, ambient temperature ESR spectra (Fig. 3). The anisotropic defects have a complicated behavior, which is not understood. The line positions and widths are strongly temperature dependent. At temperatures below 110 K, the most intensive line is at about $g=2.079$ (not shown). The low-symmetry defects in the single crystal were only observed at 9.4 GHz. In a single crystal, at 222.4 GHz, between 7.6 and 8.5 T, only an isotropic line was observed at $g=2.0006$ with a linewidth similar to the line of the powder spectra.

C. Lower limit for bulk ESR linewidth

We searched in vain for a broad line corresponding to the bulk of magnetic ions. As shown in Fig. 4, at 222.4 GHz the 20 mT broad resonance line of Mn^{2+} defect sites at g

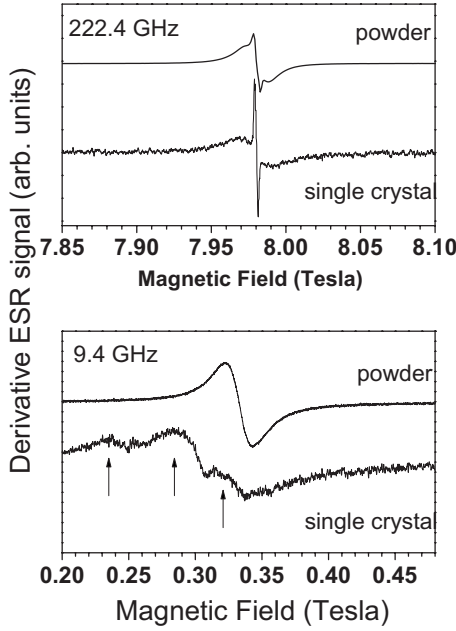


FIG. 3. ESR spectra of a PBA single crystal and powder at 222.4 GHz (top) and at 9.4 GHz (bottom) at ambient temperature. For the single-crystal spectra, the magnetic field is along a principle crystallographic axis. The weak 9.4 GHz single-crystal ESR lines, indicated by arrows, are superimposed on a broad instrumental background.

$=2.0006$ is the only observable resonance within the range of 0–9 T. Thus the ESR of the bulk is very broad: a 1 T broad resonance with the intensity of the bulk Mn^{2+} ions would have been easily detected as shown in Fig. 4.

III. DISCUSSION

A. ESR-active defects

In this and the following sections, we focus on the properties of defect sites, the reason for the absence of the ESR of the bulk is discussed in Sec. III C. The g -factor of the ESR in powders is isotropic, otherwise the line would broaden at high frequencies. In the same defects, the crystal field (zero-field splitting) is small, otherwise the low-frequency line would broaden. It is natural to assign this isotropic line to a defect with cubic symmetry. The anisotropic ESR lines in single crystals at low frequency arise from defects with lower symmetry.

We propose that the isotropic g -factor line is the ESR of C-clusters (Fig. 1) with a simple configuration of six weakly interacting Mn^{2+} ions on the cube surrounding a defect. A larger cubic cluster with many more ions cannot be entirely ruled out. H_2O molecules attached to Mn ions fill the $\text{Fe}(\text{CN})_6$ vacancy and in this environment the Mn^{2+} state is stabilized at all temperatures. The clusters have very little magnetic interaction with the surrounding lattice and the ESR is almost unaffected by the HT-LT phase transition. We do not know how this isolation is realized. The structure of the C-cluster explains qualitatively several characteristics of the ESR spectra: (i) the isotropy of the g -factor, (ii) the non-

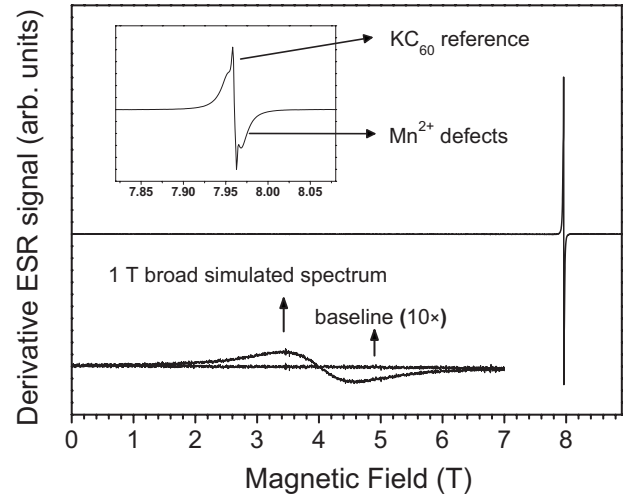


FIG. 4. 222.4 GHz ESR spectra of PBA powder at 175 K. Inset: the same spectrum zoomed around $g=2$. The flat, ten times magnified baseline, and the superimposed simulated spectra show that a 1 T broad ESR with the expected intensity would be easily detected in the 0–9 T field range.

linear variation in the line position with frequency, (iii) the temperature and frequency dependence of the linewidth, and (iv) the temperature dependence of the magnetic susceptibility of the ESR-active sites.

We first discuss (i) and (ii) which follow from the particular structure of the defect while (iii) and (iv) discussed in Sec. III B are linked to the superparamagnetism below 50 K.

The C-cluster as a whole is cubic but individual Mn^{2+} ions are not in a cubic environment since one of their six first Fe neighbors is missing. If Mn^{2+} ions in the C-cluster were isolated from each other then the crystal field (fine structure) and g -factor anisotropy would render their ESR lines strongly anisotropic. A magnetic field in a general orientation would split the ESR of C-clusters of a single crystal into three Mn^{2+} lines with different g -factors and a fine structure (and a hyperfine structure) of several lines. In the powder, the ESR of noninteracting Mn ions would be broad and frequency dependent. A coupling between Mn^{2+} ions within the C-clusters explains the observed isotropy. An isotropic exchange interaction between Mn ions, mediated by Fe, narrows the g -factor anisotropy, $\Delta g/g \cdot \nu_L$, and the fine-structure splitting, ν_D . A small exchange energy, J , is sufficient to merge all lines of a single cluster into a single isotropic line. $J > \Delta g/g \cdot h\nu_L$ and $J > h\nu_D$ are the conditions for this type of exchange narrowing.¹⁴ At high frequencies (compared to ν_D) and high temperatures ($k_B T > h\nu_L$), the crystal field (or “zero-field splitting”) does not shift the line. On the other hand, at low ESR frequencies, where ν_L and ν_D are comparable, the crystal field shifts the average line position even if the spectrum is narrowed by exchange. In second order, the fine-structure shift is on the order of ν_D^2/ν_L . The observed apparent g shift from 2.0006 at 222.4 GHz to 2.022 at 9.4 GHz corresponds to a fine-structure splitting of $|\nu_D|/\gamma = 0.07$ T if the shift is from the $-1/2 \rightarrow 1/2$ transition of Mn^{2+} ions. (The shifts of other transitions are of similar order.)

The crystal field at cluster Mn sites changes the 222.4 GHz spectra at low temperatures where $k_B T < h\nu_L$. At high

temperatures, the thermal population of Zeeman levels are not very different, thus ESR fine-structure transitions have comparable intensities. However, at low temperatures the thermal energy ($k_B T$) is smaller than the Zeeman energy and the higher Zeeman energy states are depopulated. In this case, only fine-structure transitions between the lower Zeeman energy states contribute to the spectrum. As a result, the exchange narrowed line shifts toward the fine-structure transition between the lowest-lying states.¹⁵ We have observed this shift at 222.4 GHz where $5\hbar\nu_L=40$ K is the energy of the highest Zeeman level. The resonance field of the PB powder at 25 K is down shifted 0.03 T compared to ambient temperature. As expected, this shift at 25 K and 222.4 GHz is on the order of the estimation of $|\nu_D|/\gamma=0.07$ T from the low-frequency data. From the sign of the shift we conclude that $\nu_D<0$. The complicated structure of single crystal 9.4 GHz spectra at room temperature can be caused by the crystal field and g -factor anisotropy in noncubic clusters.

As explained in Sec. III C, spin relaxation of bulk magnetic ions in the HT state is extremely fast and is without doubt even faster in the LT state. Nevertheless, the HT to LT transition changes the linewidth by only 2 mT (Fig. 2), thus C-clusters are well isolated from the bulk. A significant coupling to the bulk would result in a fast spin relaxation and a large ESR line broadening. As expected for isolated C-clusters with no phase transition; the ESR intensity is also unchanged at the HT \rightarrow LT transition.

B. Superparamagnetism

Above 50 K, the spin susceptibility of defects is to a good approximation Curie type but below 50 K, the ESR intensity increases faster than $1/T$. We argue that this is due to superparamagnetism at low temperatures where a ferromagnetic exchange between Mn ions in clusters is significant. For definitiveness, we consider the cluster of six $S=5/2$ Mn^{2+} ions coupled through 12 $S=1/2$ Fe^{3+} ions (Fig. 1), other configurations with a larger cluster size cannot be ruled out. The cluster has a common exchange narrowed resonance of all magnetic ions since the g -factor is about 2 for both Mn^{2+} and Fe^{3+} ions. An indirect Mn-Mn exchange coupling through magnetic Fe^{3+} ions is always ferromagnetic, independent of the sign of the Mn-Fe exchange. At low temperatures, the total spin of six Mn^{2+} ions is $S=15$ and the spin of the full cluster is between $S_C=21$ and $S_C=9$ for ferromagnetic and antiferromagnetic Mn-Fe coupling, respectively. Thus at low temperatures, the magnetic moment of the cluster is large and the susceptibility increases with decreasing temperature much faster than for noninteracting ions. At much higher temperatures than J , the susceptibility is about that of free Mn^{2+} ions. A Mn-Mn exchange interaction within the cluster on the order of $J=10$ K (and a much weaker interaction with the bulk) explains the ESR susceptibility.

The ferromagnetic transition of the bulk at $T_F=11$ K does not affect significantly the 9 GHz ESR intensity, which continuously increases to the lowest measurement temperature of 5 K. On the other hand, below 11 K the 9 GHz ESR linewidth increases abruptly. This is well explained with a ferromagnetic transition of the bulk at 11 K and no ferromag-

netic ordering of the superparamagnetic clusters. The cluster ESR line broadening of 14 mT below the ferromagnetic transition of the bulk arises either from long-range dipolar interactions, i.e., inhomogeneous demagnetizing fields or a small exchange coupling to the bulk. At 222.4 GHz, the ESR is centered at 8 T and demagnetizing fields have a measurable contribution to the linewidth below 25 K. In this high field, demagnetizing fields of the paramagnetic material are significant and the ferromagnetic transition is smeared and shifted to higher temperatures.

C. Absence of ESR of the bulk

We discuss the possible reasons for which only defects are ESR active and the ESR of the bulk material was not observed.

In general, to observe ESR the spin relaxation rate must be less than ν_L . The lack of a spin resonance in the LT phase is not surprising: Fe^{2+} is not magnetic and Mn^{3+} has an $S=2$ spin for which orbital effects are important. Phonons modulate the crystal field and the fast spin relaxation broadens the ESR of Mn^{3+} ions beyond observability. On the other hand, the lack of bulk ESR above the spin crossover is not easily explained. Crystals with Mn^{2+} ($S=5/2$) and Fe^{3+} ($S=1/2$) ions usually have narrow ESR lines with gyromagnetic factors near $g=2$. Fine splitting from crystal fields is relatively small for the half-filled $3d^5$ shell of Mn^{2+} . There is no zero-field splitting for $S=1/2$ Fe^{3+} ions either, the ESR of this ion is not strongly anisotropic and has been frequently observed in solids. Moreover, crystal-field anisotropy (fine-structure splitting) and the dipolar interaction are ineffective in magnetically dense systems. In PBA, the exchange interaction between Mn and Fe ions is larger than dipolar and single-ion crystal-field energies and the ESR is exchange narrowed, i.e., one expects a common Mn^{2+} and Fe^{3+} narrow ESR resonance in the bulk. Yet, we find that the ESR of the bulk of PBA is very broad, more than 1 T, i.e., at least two orders of magnitude broader than the ESR of the Mn^{2+} defect clusters in the same system. At a Larmor frequency of 9.4 GHz, a larger than 1 T linewidth means that the lifetime broadening is more than the resonance field and there is no ESR of the bulk at all.

A small admixture of the $S=2$ Mn^{3+} and $S=0$ Fe^{2+} states into the pure $S=5/2$ Mn^{2+} and $S=1/2$ Fe^{3+} states in the HT phase is the most probable explanation for this rapid spin lattice relaxation. It has been suggested in Ref. 12 that such an admixture affects the ESR of the defect line also. Charge fluctuations persisting above the LT-HT transition induce a rapid spin relaxation and consequently a very broad or non-existent ESR. This admixture was also seen by x-ray photoemission spectroscopy and Raman spectroscopy.³

IV. CONCLUSION

Single crystals of $\text{RbMn}[\text{Fe}(\text{CN})_6]\cdot\text{H}_2\text{O}$ contain ESR-active defects both with cubic and lower symmetry. At high frequency and in powders, the low-symmetry defects are not observed. The isotropic defect ESR is assigned to a cubic C-cluster of Mn^{2+} ions around $\text{Fe}(\text{CN})_6$ vacancies, which

interacts very weakly with the bulk. At low temperatures, the C-clusters are superparamagnetic but they do not order at the $T_F=11$ K ferromagnetic transition of the bulk. We suggest that the electronic configuration at high temperatures is not a pure configuration of Mn^{2+} and Fe^{3+} ions but has an admixture of Mn^{3+} and Fe^{2+} states of the low-temperature phase. This is the reason for the lack of an observable ESR of Mn^{2+} and Fe^{3+} ions in the bulk.

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APPENDIX

The composition of the powdered sample was $(Rb_{0.91}Mn[Fe(CN)_6]_{0.97} \cdot 1.53H_2O)$. A solution of 0.495 g $MnCl_2 \cdot 4H_2O$ in 25 mL of H_2O was added to a mixed solution of 0.823 g $K_3[Fe(CN)_6]$ and 3.023 g $RbCl$ in 25 mL of H_2O . The addition speed was kept constant at 6 mL h^{-1} with a syringe pump (Sage Instruments, model 352). The solution was stirred at a constant rate of 5.5 rps. The temperature of the combined solution was kept constant at 318 K with a water bath. A brown powder precipitated which was centrifuged and washed twice with distilled water of room temperature. The samples were dried overnight in vacuum. Elemental analysis was performed at the analysis facility of CNRS in Vernaison, France. Calculated for $Rb_{0.91}Mn[Fe(CN)_6]_{0.97} \cdot 1.53H_2O$: Rb 21.26%, Mn 15.03%, Fe 14.80%, C 19.10%, N 22.27%, and H 0.84%. Found: Rb 21.26%, Mn 15.03%, Fe 14.80%, C 20.23%, N 22.63%, and H 0.32%. Yield (based on Mn): 84%.

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